# Multi-agent Dynamic Resource Allocation: A Reinforcement Learning Approach

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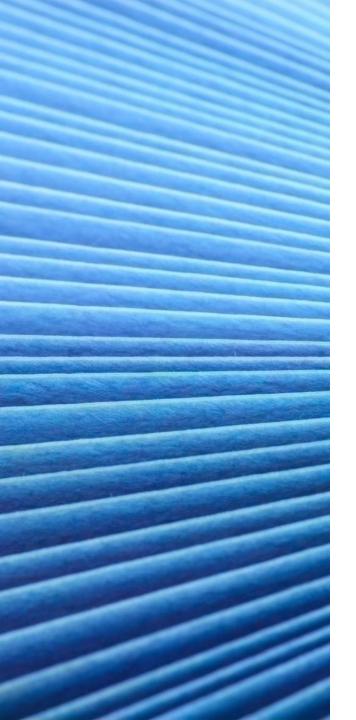
International Joint Workshop of Artificial Intelligence for Healthcare (HC@AIxIA) and HYbrid Models for Coupling Deductive and Inductive ReAsoning (HYDRA):

HC@AlxIA+HYDRA 2025

co-located with

The 28th European Conference on Artificial Intelligence (ECAI 2025)

Bologna, Italy, October 25-26, 2025



#### Aim of this work

Study of cooperative resource allocation in multi-agent systems (hospital networks).

Agents redistribute limited resources (doctors) respecting local constraints and global objectives.

Dynamic scenario: staffing requirements vary over time.

#### Motivation

Fair allocation is crucial in decentralized systems (e.g., healthcare).

Hospitals may lend staff during emergencies.

Limitations of existing approaches [a]: they focus on a static scenario.



# Proposed Approach (Overview)

A **Reinforcement Learning (RL)** approach based on Proximal Policy Optimisation (PPO).

**Reward** composed of three terms, which penalize, respectively:

- Deviation from the target staffing level of every hospital.
- Violation of the minimum staffing level needed by each hospital to operate effectively.
- Imbalance of the resulting staffing levels.

## Problem definition

#### Input:

Hospitals  $H = {\vec{h}_1, ..., \vec{h}_n}$ 

Each  $\vec{h}_i$  described by:

- $c_i$ : current #doctors
- *t<sub>i</sub>*: target #doctors
- $m_i$ : minimum #doctors

**Objective**: transfer doctors from a hospital to another such that :

- $y_i$  is as close as possible to  $t_i$
- $y_i < m_i$  arises the least possible
- the various  $|y_i c_i|$ 's are as much similar to each other as possible

 $(y_i: \text{\#doctors of } \vec{h}_i \text{ after the transfer})$ 

## A **Reinforcement Learning (RL)** approach which maximizes the following reward:

$$\mathcal{R} = -\underbrace{\sum_{i=1}^{n} (y_i - t_i)^2}_{\text{target error}} - \underbrace{\eta \sum_{i=1}^{n} \max(0, m_i - y_i)}_{\text{minima violations}} - \underbrace{\sigma^2(a)}_{\text{fairness}}$$

## Proposed method

**Target error**: deviation from target, i.e., the reward penalizes configurations where the current allocation of doctors is far from the desired target distribution.

**Minima violations**: heavy penalties are given if any hospital drops below its minimum number of staff units needed to guarantee its operation.

**Fairness** in transfer procedures: uneven transfers of doctors discouraged; the imbalance of the entire re-allocation process is quantified by the variance of the distribution of doctors across the various hospitals.

### Experiments

150 synthetically-generated hospitals; random  $c_i$ ,  $m_i$ ,  $t_i$ ; repeated 20 times for robustness.

#### **Metrics:**

- Mean Absolute Error (Target Deviation)

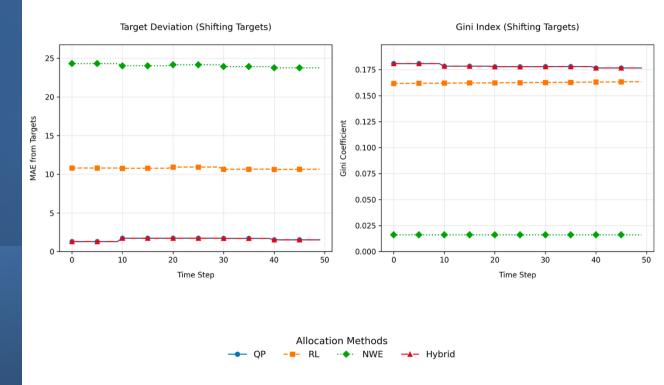
$$ext{MAE} = rac{1}{N} \sum_{i=1}^{N} |y_i - t_i|$$

- **Gini Index** (inequality)

$$\mathcal{G} = \frac{1}{N} \left( N + 1 - 2 \sum_{i=1}^{N} \frac{\sum_{j=1}^{i} y_j}{\sum_{j=1}^{N} y_j} \right)$$

Compared the **proposed RL approach** to **existing methods** for the **static** scenario (QP, NWO, Progressive Taxation, Hybrid [a]).

# Results: Shifting Targets scenario

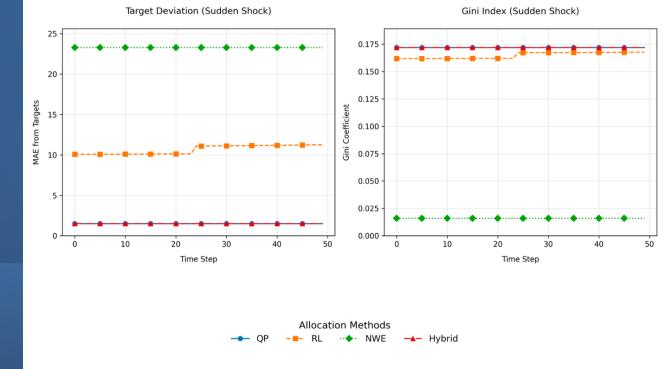


(a) Average Target Deviation (MAE) and Gini Index of the RL (proposed), NWO, QP, Hybrid (baselines) strategies in the Shifting Targets scenario.

#### **Shifting Targets scenario:**

hospital-specific targets undergo minor adjustments (loses or gains at most two doctors) every 10 time steps (overall time horizon: 50 time steps).

### Results: Sudden Shock scenario

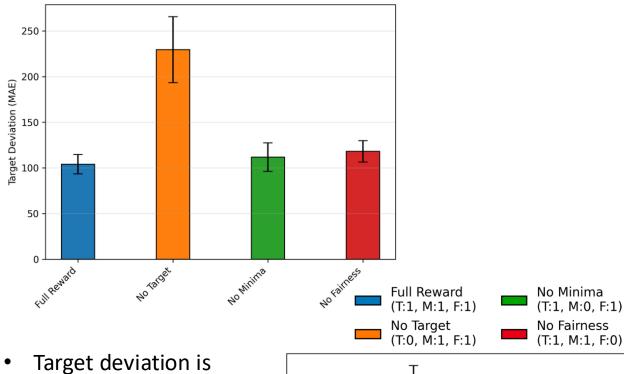


(b) Average Target Deviation (MAE) and Gini Index of the RL (proposed), NWO, QP, Hybrid (baselines) strategies in the Sudden Shock scenario.

#### **Sudden Shock scenario:**

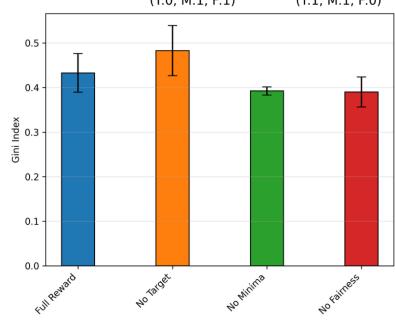
one hospital loses half its workforce at the midpoint of the time horizon.

# Results: ablation study



Target deviation is the most impactful component.

 Removal of minimum or fairness component leads to a lower Gini Index but at the price of a consistent drop of MAE.





#### Conclusions

- Tackled the problem of cooperative resource allocation in multi-agent systems (hospital networks).
- Advanced the state of the art by handling a dynamic scenario where staffing requirements vary over time.
- Devised a reinforcement learning approach to tackle the target problem.
- Performed experiments to assess the relevance of the proposed method.



## Thanks!

Questions?