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#### **DS 2022**

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# When Correlation Clustering Meets Fairness Constraints

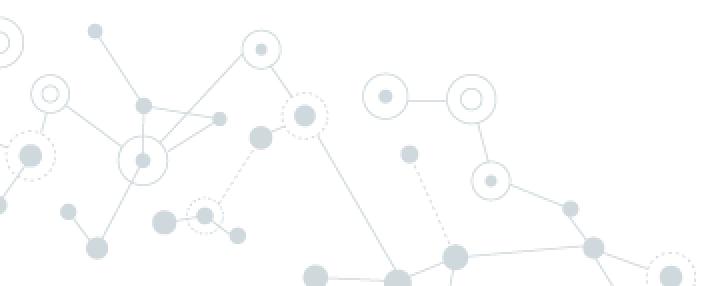
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### Today's Menu

- Intro to the context
- Background on Correlation Clustering
- The Fair-CC Problem
- Proposed approach
- Fairness-aware evaluation metrics
- Experimental methodology and results
- Conclusions and Future Work



#### Introduction

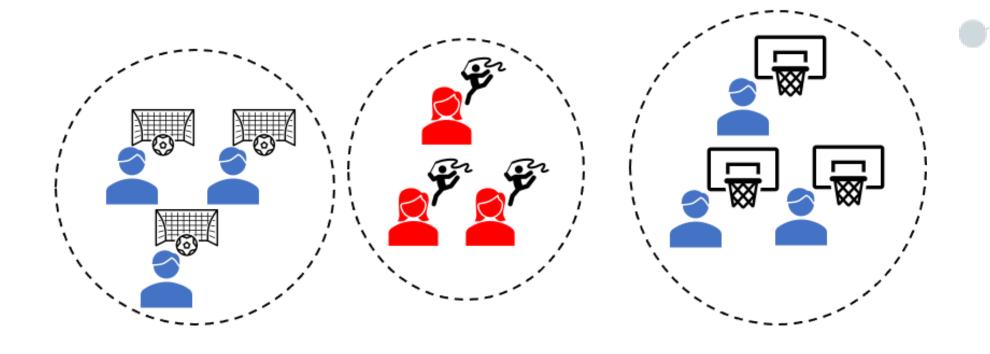
- Machine Learning (ML) systems achieved decisionmaking power in our lives (shall we entrust them?)
- Input data is often (intrinsically) biased
- ML algorithms must avoid amplifying input data bias
- Disparate impact must be removed
  - no group of individuals should (even indirectly) be discriminated by a decision-making system [1]

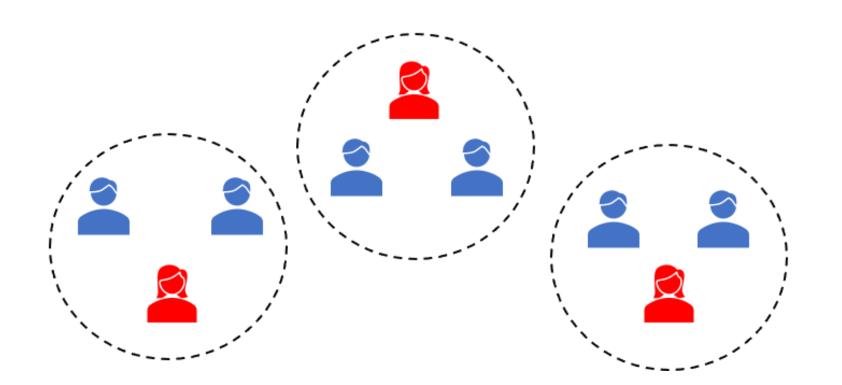


# The Fair Clustering Problem

#### Clustering a set of data objects s.t.:

- Similar objects are assigned to the same cluster, whereas dissimilar objects are assigned to different clusters
- Clusters should not be dominated by a specific type of sensitive data class (e.g., people having the same sex)







Can we tackle this problem through a

correlation clustering framework?

# Min-Disagreement Correlation Clustering (MIN-CC)

Given an undirected graph  $G = \langle V, E \rangle$  with vertex set V and edge set  $E \subseteq V \times V$ , and weights  $w_{uv}^+, w_{uv}^- \in \mathbf{R}_0^+$ , for all edges  $(u, v) \in E$ , find a clustering  $C: V \longrightarrow \mathbf{N}^+$  that minimizes:

$$\sum_{(u,v)\in E,\mathcal{C}(u)=\mathcal{C}(v)} w_{uv}^{-} + \sum_{(u,v)\in E,\mathcal{C}(u)\neq\mathcal{C}(v)} w_{uv}^{+}$$

where  $w_{uv}^+$ , resp.  $w_{uv}^-$ , denote the benefit of clustering u and v together, resp. separately.



#### Problem Statement - Notation

Let  $\mathcal{X} = \{X_1, \dots, X_n\}$  be a set of n objects defined over a set of attributes  $\mathcal{A}$  divided into two sets:

- $\mathcal{A}^F$  containing *fairness-aware* (or *sensitive*) attributes (e.g., those identifying sex, race, religion, relationship status in a citizen database);
- $\mathcal{A}^{\neg F}$  containing *non-sensitive* attributes (e.g., user preferences).

Both can include numerical (N) and categorical (C) attributes:

$$\mathcal{A}^F = \mathcal{A}_N^F \cup \mathcal{A}_C^F, \qquad \mathcal{A}^{\neg F} = \mathcal{A}_N^{\neg F} \cup \mathcal{A}_C^{\neg F}$$



#### Problem Statement - Fair-CC

Given a set of objects  $\mathcal{X}$ , two sets of attributes  $\mathcal{A}^F$  and  $\mathcal{A}^{\neg F}$ , and an object similarity function  $sim_S(\cdot)$  defined over the subspace S of the attribute set, find a clustering  $\mathcal{C}^*$  to minimize:

$$\sum_{u,v \in \mathcal{X}, \mathcal{C}(u) = \mathcal{C}(v)} sim_{\mathcal{A}^F}(u,v) + \sum_{u,v \in \mathcal{X}, \mathcal{C}(u) \neq \mathcal{C}(v)} sim_{\mathcal{A}^{\neg F}}(u,v)$$

This corresponds to solving a complete Min-CC instance:

- $\odot$  The set of vertices corresponds to the objects in  ${\mathcal X}$  and,
- $\odot$  For each pair of vertices u and v, the positive-type (resp. negative-type) correlation-clustering weight corresponds to the similarity score between the two vertices according to the non-sensitive (resp. sensitive) attributes.

# Utility functions

$$sim_{\mathcal{A}^{\neg F}}(u,v) := \psi^{+}(\alpha_{N}^{\neg F} \cdot sim_{\mathcal{A}^{\neg F}_{N}}(u,v) + (1-\alpha_{N}^{\neg F}) \cdot sim_{\mathcal{A}^{F}_{C}}(u,v) \cdot sim$$

$$\alpha_N^F = |\mathcal{A}_N^F|/(|\mathcal{A}_N^F| + |\mathcal{A}_C^F|)$$

$$\alpha_N^{\neg F} = |\mathcal{A}_N^{\neg F}|/(|\mathcal{A}_N^{\neg F}| + |\mathcal{A}_C^{\neg F}|)$$

Weight similarities proportionally to the number of involved attributes

$$\psi^{+} = exp(|\mathcal{A}^{F}|/(|\mathcal{A}^{F}| + |\mathcal{A}^{\neg F}|) - 1)$$
  
$$\psi^{-} = exp(|\mathcal{A}^{\neg F}|/(|\mathcal{A}^{F}| + |\mathcal{A}^{\neg F}|) - 1)$$

Smoothing factors to penalize weights that are computed on a small number of attributes



# Solving Fair-CC

The CC-Bounds algorithm: [2]

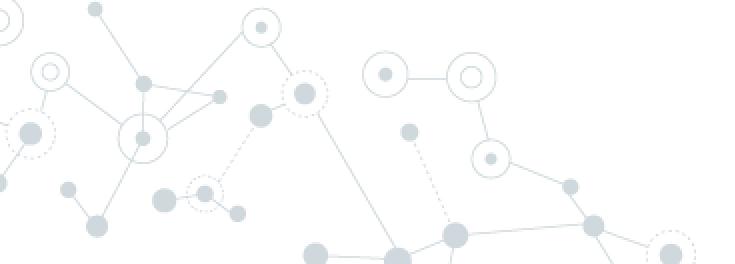
Input: Set of objects  $\mathcal{X}$ , sensitive attributes  $\mathcal{A}^F$ , non-sensitive attributes  $\mathcal{A}^{\neg F}$ , Min-CC algorithm A

Output: Clustering  ${\mathcal C}$  of  ${\mathcal X}$ 

- 1. Compute  $sim_{\mathcal{A}^{\neg F}}(u, v)$ ,  $sim_{\mathcal{A}^{F}}(u, v) \ \forall u, v \in \mathcal{X}$
- 2. Build the instance

$$I = \langle G = (\mathcal{X}, \mathcal{X} \times \mathcal{X}), \{sim_{\mathcal{A}^{\neg F}}(u, v), sim_{\mathcal{A}^{F}}(u, v)\}_{u, v \in \mathcal{X} \times \mathcal{X}} \rangle$$

3.C ←run A on I



[2] Mandaglio, D., Tagarelli, A., Gullo, F.: Correlation clustering with global weight bounds. In: Proc. ECML-PKDD Conf. pp. 499–515 (2021)

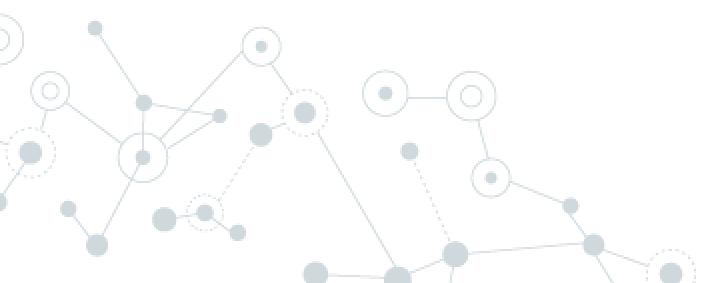
#### Theoretical remarks

Let  $T_A(\mathcal{X})$  the running time of the algorithm A on the set of data objects  $\mathcal{X}$ 

- The time complexity of CCBounds is  $\mathcal{O}(|\mathcal{X}|^2|\mathcal{A}| + T_A(\mathcal{X}))$ 
  - Compute similarities over  $\mathcal A$  attributes, for each pair of objects in  $\mathcal X$ , then solve the resulting Min-CC instance through A
- The space complexity of CC-Bounds is  $\mathcal{O}(|\mathcal{X}|^2)$ 
  - In-memory similarity storing

The Min-CC algorithm A used in CC-Bounds is the one proposed in [3], as it proposes constant-factor approximation guarantees (under certain conditions), s.t.  $T_A(\mathcal{X}) = \mathcal{O}(|\mathcal{X}|^2)$ .

✓ The time complexity of CCBounds become  $\mathcal{O}(|\mathcal{X}|^2|\mathcal{A}|)$ .



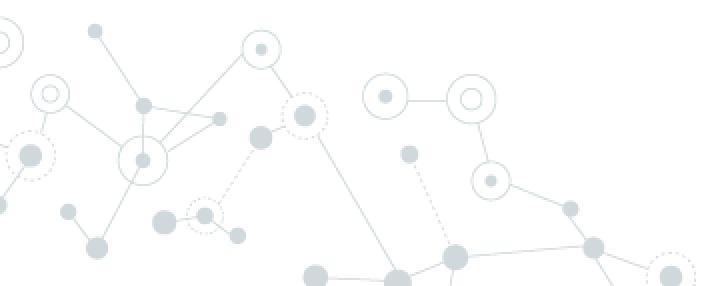
#### Theorem 1 [2]

If the condition

$$\begin{pmatrix} |\mathcal{X}| \\ 2 \end{pmatrix}^{-1} \left( sim_{\mathcal{A}^{\neg F}}(u, v) + sim_{\mathcal{A}^{F}}(u, v) \right)$$

$$\geq \max_{u, v \in \mathcal{X}} \left| sim_{\mathcal{A}^{\neg F}}(u, v) - sim_{\mathcal{A}^{F}}(u, v) \right|$$

holds on the similarity scores and the oracle A is an  $\alpha$ -approximation algorithm for Min-CC, CCBounds is  $\alpha$ -approximation algorithm for Fair-CC.



### **Evaluating Fairness**

Focus on algorithm-independent evaluation metrics following a *group-level* approach under the *disparate impact* doctrine <sup>[4]</sup>

$$balance(\mathcal{C})^{[5,6]} = \min_{C \in \mathcal{C}, b \in [m]} \min\{R_{C,b}, \frac{1}{R_{C,b}}\} \in [0,1]$$

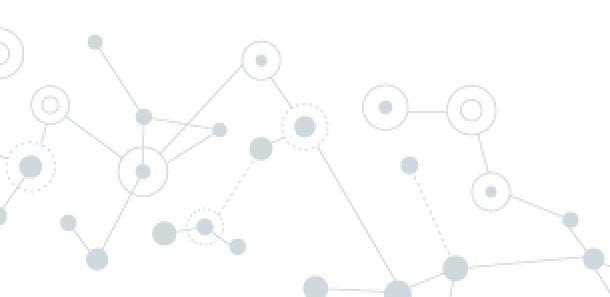
$$AE_{A}(C_{0}) = \frac{\sum_{C \in C} |C| \times ED(C_{A}, \mathcal{X}_{A})}{\sum_{C \in C} |C|}$$

[4] Feldman, M., Friedler, S.A., Moeller, J., Scheidegger, C., Venkatasubramanian, S.: Certifying and removing disparate impact. In: Proc. ACM KDD Conf. pp. 259–268 (2015)

[5] Chierichetti, F., Kumar, R., Lattanzi, S., Vassilvitskii, S.: Fair clustering through fairlets. In: Proc. NIPS Conf. pp. 5029–5037 (2017)

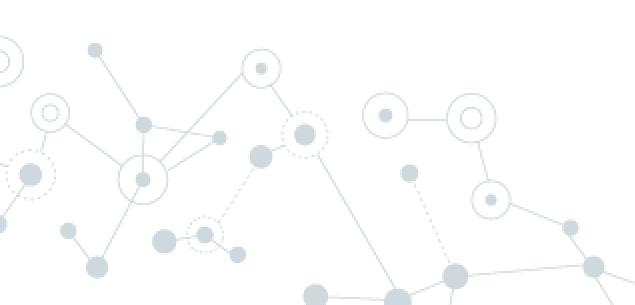
[6] Bera, S.K., Chakrabarty, D., Flores, N., Negahbani, M.: Fair algorithms for clustering. In: Proc. NIPS Conf. pp. 4955–4966 (2019)

[7] Abraham, S.S., P, D., Sundaram, S.S.: Fairness in clustering with multiple sensitive attributes. In: Proc. EDBT Conf. pp. 287–298 (2020)



# Competing methods

- Fair Clustering through Fairlets [5]
- HST-based Fair Clustering [8]
- Fair Correlation Clustering [9]
- Based on fairlets decomposition (direct or via correlation clustering)
- The first two can just handle a single sensitive attribute





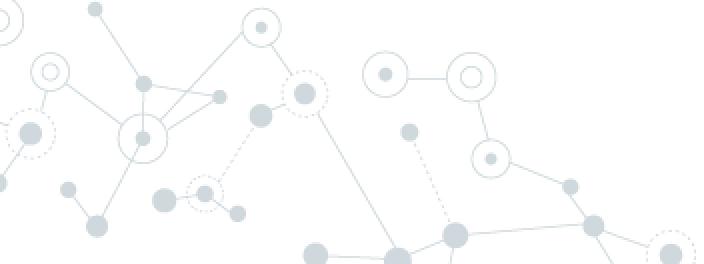
<sup>[8]</sup> Backurs, A., Indyk, P., Onak, K., Schieber, B., Vakilian, A., Wagner, T.: Scalable fair clustering. In: Proc. ICML Conf. pp. 405–413 (2019)

[9] Ahmadian, S., Epasto, A., Kumar, R., Mahdian, M.: Fair correlation clustering. In: Proc. AISTATS Conf. pp. 4195–4205 (2020)

#### Data

- Publicly available real-world relational datasets
- Focus on a smaller subset of the original attributes

	#objs.	$\frac{sensitive}{\text{attribute}}$	non-sensitive $attributes$
$oxed{Adult}$	48 842	sex	age, fnlgwt, education_num, capital_gain, hours_per_week
Bank	40 004	marital	age, balance, duration
CreditCard	10 127	sex	customer_age, dependent_count, avg_utilization_ratio, total_relationship_count
Diabetes	101 763	sex	age, time_in_hospital
Student	649	sex	$age, study\_time, absences$

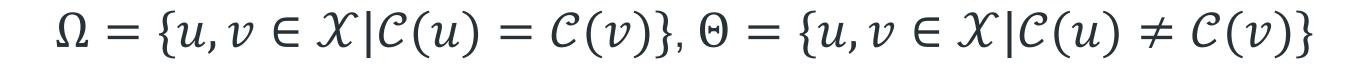


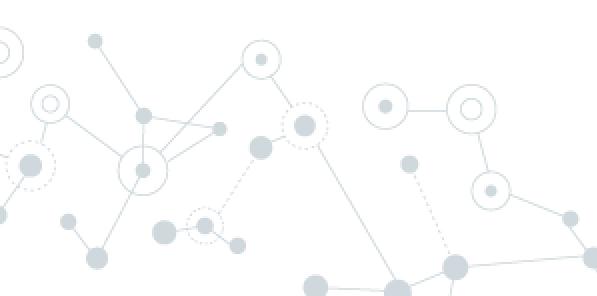
# Evaluation goals

$$inter(\mathcal{A}^{\neg F}) = \frac{1}{|\Theta|} \sum_{u,v \in \Theta} sim_{\mathcal{A}^{\neg F}}(u,v)$$

$$inter(\mathcal{A}^{F}) = \frac{1}{|\Theta|} \sum_{u,v \in \Theta} sim_{\mathcal{A}^{F}}(u,v)$$

Running times were measured while executing on the *Cresco6* cluster\*

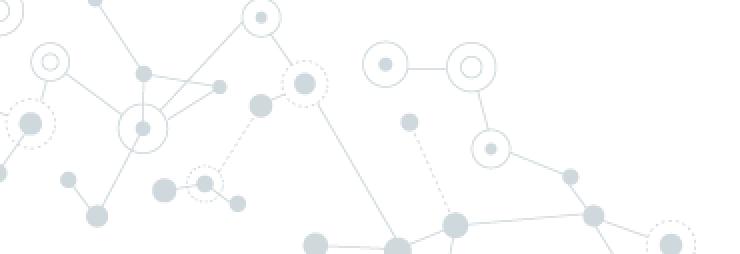




# Hyper-params and Configurations

- Random sampling of the original data
- 1k/10k tuples which preserve some desired ratio between the protected classes
- Specification of p and q parameters
  - p/q represents the minimum balance required by each cluster
- Minimum shared requirements, e.g., single and binary sensitive attribute
- Number of clusters k as the (rounded) avg.
   number of clusters returned by CCBounds in ten iterations

	p,q	split ratio	$k_{avg}$	k
Adult-1k	1,2	650/350	3.12	3
Bank-1k	1,2	650/350	3.48	$\mid 3 \mid$
$Credit ext{-} Card ext{-} 1k$	1,6	800/200	5.6	$\mid 6 \mid$
Diabetes-1 $k$	1,2	540/460	5.2	5
Student-1 $k$	1,2	266/383	3.88	4
Adult-10k	1,2	6500/3500	2.96	3
Bank-10k	1,2	6500/3500	3.28	$\mid 3 \mid$
$Credit ext{-} Card ext{-} 10k$	1,6	4769/5358	6.32	$\mid 6 \mid$
Diabetes-10 $k$	1,2	5400/4600	6.44	$\mid 6 \mid$
Adult-Full	2,5	32650/16192	3.64	4
$Bank ext{-}Full$	2,5	12790/27214	3.64	4
$Diabetes ext{-}Full$	1,2	47 055/54 708	OOM	6



#### Results - Balance

		#clust.	balance ↑	AE↓	$intra(\mathcal{A}^{ eg F}) \uparrow$	$igg intra(\mathcal{A}^F)\downarrow igg $	$inter(\mathcal{A}^{\neg F})\downarrow$	$inter(\mathcal{A}^F) \uparrow$	time (s) \
	CCBounds	3.12	0.565	0.007	0.685	0.524	0.415	0.334	< 1
A d1+ 11-	FAIRLETS	3	0.805	0.004	0.585	0.319	0.596	0.335	< 1
Adult-1k	HST-FC	3	0.971	0.01	0.616	0.335	0.599	0.336	< 1
	SIGNED	41	0.66	0.03	0.59	0.32	0.60	0.33	240
	CCBounds	2.96	0.52	0.03	0.65	0.43	0.43	0.33	3.86
A Jl+ 10l+	FAIRLETS	3	0.82	0.003	0.60	0.32	0.615	0.33	< 1
Adult-10k	HST-FC	3	0.98	0.006	0.626	0.336	0.618	0.336	3.03
	SIGNED	NA	NA	NA	NA	NA	NA	NA	> 48h
	CCBounds	3.64	0.56	0.003	0.69	0.47	0.42	0.24	75.5
Adult-Full	FAIRLETS	4	0.66	0.02	0.59	0.32	0.62	0.34	6.5
	HST-FC	4	0.96	0.008	0.63	0.34	0.62	0.34	72.86
	SIGNED	NA	NA	NA	NA	NA	NA		>48h
	CCBounds	3.48	0.565	0.006	0.727	0.587	0.441	0.369	< 1
Danle 11e	FAIRLETS	3	0.828	0.002	0.606	0.354	0.613	0.364	< 1
Bank-1k	HST-FC	3	0.968	0.007	0.621	0.365	0.617	0.33 0.33 0.336 NA 0.24 0.34 0.34 NA 0.369	< 1
	SIGNED	41	0.7	0.03	0.61	0.35	0.63		224
	CCBounds	3.28	0.52	0.0007	0.78	0.63	0.45	0.36	4.74
Bank-10k	FAIRLETS	3	0.7	0.001	0.59	0.32	0.63	0.36	< 1
Dank-10k	HST-FC	3	0.969	0.004	0.656	0.365	0.656	0.365	3.07
	SIGNED NA NA NA	NA	NA	NA	NA	NA	>48h		
	CCBounds	3.64	0.55	0.0004	0.72	0.55	0.45	0.37	51.1
Ponk Full	FAIRLETS	4	0.68	0.001	0.62	0.34	0.65	0.36	5.3
Bank-Full	HST-FC	4	0.94	0.008	0.66	0.37	0.66	0.37	28
	SIGNED	NA	NA	NA	NA	NA	NA	NA	> 48h

- "Fairness-native" methods yield better balance scores
- CCBounds is aligned with its direct competing method in most cases
- On small yet heavily unbalanced datasets (i.e., CreditCard-1k with an 80:20 ratio), CCBounds achieves the second-best score, while other competing methods struggle
- Overall, the balance obtained by CCBounds in all evaluation scenarios ranges from 0.45 to 0.613

#### Results - Balance

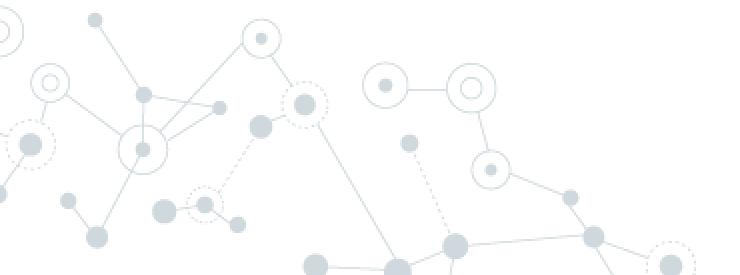
		#clust.	balance ↑	$\mathrm{AE}\downarrow$	$intra(\mathcal{A}^{ eg F})\uparrow$	$\left intra(\mathcal{A}^F)\downarrow ight $	$inter(\mathcal{A}^{\lnot F})\downarrow$	$inter(\mathcal{A}^F)\uparrow$	time (s) $\downarrow$
	CCBounds	5.6	0.613	0.127	0.6	0.497	0.46	0.362	< 1
Cradit Cand 11	FAIRLETS	6	0.4	0.042	0.485	0.355	0.486	0.375	< 1
CreditCard-1k	HST-FC	6	0.756	0.026	0.513	0.373	0.481	0.377	< 1
	Signed	171	0.56	0.1	0.56	0.41	0.49	0.38	173
	CCBounds	6.32	0.496	0.17	0.6	0.46	0.46	0.32	4.1
CreditCard-10k	FAIRLETS	6	0.94	0.01	0.497	0.34	0.49	0.337	< 1
CreditCard-10k	HST-FC	6	0.955	0.013	0.52	0.337	0.491	0.337	2.52
	SIGNED	NA	NA	NA	NA	NA	NA	NA	$>48\mathrm{h}$
	CCBounds	5.2	0.45	0.33	0.622	0.519	0.512	0.352	< 1
D' 1 11	FAIRLETS	5	0.92	0.015	0.537	0.381	0.532	0.385	< 1
Diabetes-1k	HST-FC	5	0.872	0.05	0.585	0.386	0.529	0.386	< 1
	SIGNED	106	0.85	0.04	0.58	0.36	0.54	0.386 0.38 0.36	257
	CCBounds	6.44	0.48	0.22	0.65	0.54	0.5		4.72
Diabatas 101	FAIRLETS	6	0.92	0.01	0.53	0.38	0.53	0.39	< 1
Diabetes-10k	HST-FC	6	0.799	0.065	0.59	0.388	0.53	0.386	2.84
	Signed	NA	NA	NA	NA	NA	NA	0.377 0.38 0.32 0.337 0.337 NA 0.352 0.385 0.386 0.38 0.36 0.39 0.386 NA OOM OOM OOM OOM OOM OOM OOM	$>48\mathrm{h}$
	CCBounds	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
Diabetes-Full	FAIRLETS	6	0.93	0.01	OOM	OOM	OOM	OOM	22.2
Diabetes-ruii	HST-FC	6	0.81	0.06	OOM	OOM	OOM	OOM	761.2
	SIGNED	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
	CCBounds	3.88	0.51	0.10	0.625	0.463	0.471	0.224	< 1
Ctudont 11-	FAIRLETS	4	0.82	0.013	0.528	0.339	0.543	0.357	< 1
Student-1k	HST-FC	4	0.93	0.024	0.563	0.357	0.541	0.358	< 1
	SIGNED	55	0.82	0.04	0.57	0.34	0.55	0.36	71

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- CCBounds is aligned with its direct competing method in most cases
- On small yet heavily unbalanced datasets (i.e., CreditCard-1k with an 80:20 ratio), CCBounds achieves the second-best score, while other competing methods struggle
- Overall, the balance obtained by CCBounds in all evaluation scenarios ranges from 0.45 to 0.613

# Results - Average Euclidean Fairness

		#clust.	balance ↑	$ ext{AE}\downarrow$	$intra(\mathcal{A}^{ eg F}) \uparrow$	$\Big  intra({\cal A}^F) \downarrow$	$inter(\mathcal{A}^{ eg F})\downarrow$	$inter(\mathcal{A}^F) \uparrow$	time (s)
	CCBounds	3.12	0.565	0.007	0.685	0.524	0.415	0.334	< 1
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	SIGNED	NA	NA	NA	NA	NA	NA	NA	> 48h
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Adult-Full	FAIRLETS	4	0.66	0.02	0.59	0.32	0.62	0.34	6.5
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	SIGNED	NA	NA	NA	NA	NA	NA	NA	> 48h
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Dank-run	HST-FC	4	0.94	0.008	0.66	0.37	0.66	0.37	28
	SIGNED	NA	NA	NA	NA	NA	NA	NA	> 48h

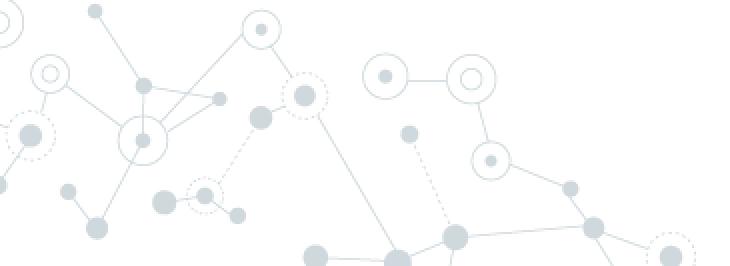
- CCBounds obtains very good scores under different scenarios
- Among the best-performing approaches for the Adult-1k, Adult-Full and Bank-1k datasets
- Outperforms all the other methods by an order of magnitude on Bank-10k and Bank-Full
- Performances worsen while considering the remaining datasets



# Results - Average Euclidean Fairness

		#clust.	balance ↑	$\mathrm{AE}\downarrow$	$intra(\mathcal{A}^{ eg F}) \uparrow$	$\left intra(\mathcal{A}^F)\downarrow ight $	$\left inter(\mathcal{A}^{ eg F})\downarrow ight $	$inter(\mathcal{A}^F)\uparrow$	time (s) ↓
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Credit Card-10k	HST-FC	6	0.955	0.013	0.52	0.337	0.491	0.337	2.52
	SIGNED	NA	NA	NA	NA	NA	NA	NA	$>48\mathrm{h}$
	CCBounds	5.2	0.45	0.33	0.622	0.519	0.512	0.352	< 1
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	SIGNED	106	0.85	0.04	0.58	0.36	0.54	0.352 <b>0.385</b>	257
	CCBounds	6.44	0.48	0.22	0.65	0.54	0.5	0.36	4.72
D:-b-+ 10l-	FAIRLETS	6	0.92	0.01	0.53	0.38	0.53	0.39	< 1
Diabetes-10k	HST-FC	6	0.799	0.065	0.59	0.388	0.53	0.386	2.84
	SIGNED	NA	NA	NA	NA	NA	NA	NA	> 48h
	CCBounds	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
Diahataa Eull	FAIRLETS	6	0.93	0.01	OOM	OOM	OOM	OOM	22.2
Diabetes-Full	HST-FC	6	0.81	0.06	OOM	OOM	OOM	OOM	761.2
	SIGNED	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
	CCBounds	3.88	0.51	0.10	0.625	0.463	0.471	0.224	< 1
C414 11-	FAIRLETS	4	0.82	0.013	0.528	0.339	0.543	0.357	< 1
Student-1k	HST-FC	4	0.93	0.024	0.563	0.357	0.541	0.358	< 1
	SIGNED	55	0.82	0.04	0.57	0.34	0.55	0.36	71

- CCBounds obtains very good scores under different scenarios
- Among the best-performing approaches for the *Adult-1k*, *Adult-Full* and *Bank-1k* datasets
- Outperforms all the other methods by an order of magnitude on *Bank-10k* and *Bank-Full*
- Performances worsen while considering the remaining datasets



#### Results - Similarities

		#clust.	balance ↑	$ ext{AE}\downarrow$	$intra(\mathcal{A}^{ eg F})\uparrow$	$\Big  intra(\mathcal{A}^F) \downarrow \Big $	$\left inter(\mathcal{A}^{ eg F})\downarrow ight $	$inter(\mathcal{A}^F) \uparrow$	time (s) $\downarrow$
	CCBounds	3.12	0.565	0.007	0.685	0.524	0.415	0.334	< 1
A dl+ 11-	FAIRLETS	3	0.805	0.004	0.585	0.319	0.596	0.335	< 1
Adult-1k	HST-FC	3	0.971	0.01	0.616	0.335	0.599	0.336	< 1
	SIGNED	41	0.66	0.03	0.59	0.32	0.60	0.33	240
	CCBounds	2.96	0.52	0.03	0.65	0.43	0.43	0.33	3.86
Adult-10k	FAIRLETS	3	0.82	0.003	0.60	0.32	0.615	0.33	< 1
Adult-10k	HST-FC	3	0.98	0.006	0.626	0.336	0.618	0.336	3.03
	SIGNED	NA	NA	NA	NA	NA	NA	NA	$>48\mathrm{h}$
	CCBounds	3.64	0.56	0.003	0.69	0.47	0.42	0.24	75.5
Adult-Full	FAIRLETS	4	0.66	0.02	0.59	0.32	0.62	0.34	6.5
	HST-FC	4	0.96	0.008	0.63	0.34	0.62	0.34	72.86
	SIGNED	NA	NA	NA	NA	NA	NA		>48h
	CCBounds	3.48	0.565	0.006	0.727	0.587	0.441	0.369	< 1
Bank-1k	FAIRLETS	3	0.828	0.002	0.606	0.354	0.613	0.364	< 1
рапк-тк	HST-FC	3	0.968	0.007	0.621	0.365	0.617	0.365	< 1
	SIGNED	41	0.7	0.03	0.61	0.35	0.63	0.36	224
	CCBounds	3.28	0.52	0.0007	0.78	0.63	0.45	0.36	4.74
Bank-10k	FAIRLETS	3	0.7	0.001	0.59	0.32	0.63	0.36	< 1
Dank-10k	HST-FC	3	0.969	0.004	0.656	0.365	0.656	0.365	3.07
	SIGNED	NA	NA	NA	NA	NA	NA	NA	$>48\mathrm{h}$
	CCBounds	3.64	0.55	0.0004	0.72	0.55	0.45	0.37	51.1
Bank-Full	FAIRLETS	4	0.68	0.001	0.62	0.34	0.65	0.36	5.3
Dank-run	HST-FC	4	0.94	0.008	0.66	0.37	0.66	0.37	28
	SIGNED	NA	NA	NA	NA	NA	NA	NA	$>48\mathrm{h}$

- On the sensitive attributes,
  CCBounds tends to group a few
  more objects with the same sensitive
  attribute value than the other
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- CCBounds is still able to properly separate the objects into clusters, when accounting for the sensitive attribute
  - CCBounds achieves the best performance in all the considered evaluation scenarios when considering non-sensitive attributes

#### Results - Similarities

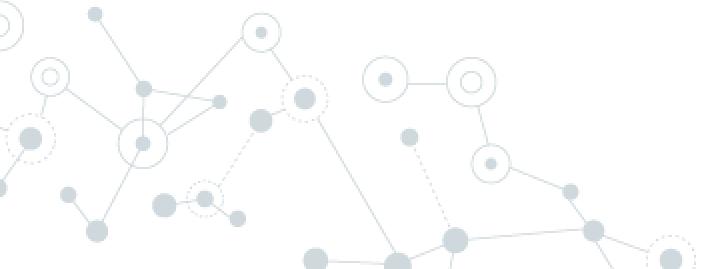
		#clust.	balance ↑	$\mathrm{AE}\downarrow$	$intra(\mathcal{A}^{ eg F})\uparrow$	$intra(\mathcal{A}^F)\downarrow$	$inter(\mathcal{A}^{ eg F})\downarrow$	$inter(\mathcal{A}^F)\uparrow$	time (s) $\downarrow$
	CCBounds	5.6	0.613	0.127	0.6	0.497	0.46	0.362	< 1
CreditCard-1k	FAIRLETS	6	0.4	0.042	0.485	0.355	0.486	0.375	< 1
CreditCard-1k	HST-FC	6	0.756	0.026	0.513	0.373	0.481	0.377	< 1
	SIGNED	171	0.56	0.1	0.56	0.41	0.49	0.38	173
	CCBounds	6.32	0.496	0.17	0.6	0.46	0.46	0.32	4.1
CreditCard-10k	FAIRLETS	6	0.94	0.01	0.497	0.34	0.49	0.337	< 1
CreditCard-10k	HST-FC	6	0.955	0.013	0.52	0.337	0.491	0.337	2.52
	SIGNED	NA	NA	NA	NA	NA	NA	NA	>48h
	CCBounds	5.2	0.45	0.33	0.622	0.519	0.512	0.352	< 1
Diabetes-1k	FAIRLETS	5	0.92	0.015	0.537	0.381	0.532	0.385	< 1
	HST-FC	5	0.872	0.05	0.585	0.386	0.529	0.386	< 1
	SIGNED	106	0.85	0.04	0.58	0.36	0.54	0.38	257
	CCBounds	6.44	0.48	0.22	0.65	0.54	0.5	0.36	4.72
Diabatas 101.	FAIRLETS	6	0.92	0.01	0.53	0.38	0.53	0.39	< 1
Diabetes-10k	HST-FC	6	0.799	0.065	0.59	0.388	0.53	0.386	2.84
	SIGNED	NA	NA	NA	NA	NA	NA	NA	>48h
	CCBounds	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
Diabetes-Full	FAIRLETS	6	0.93	0.01	OOM	OOM	OOM	OOM	22.2
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	SIGNED	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
	CCBounds	3.88	0.51	0.10	0.625	0.463	0.471	0.224	< 1
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# Results - Running Times

		#clust.	balance ↑	$ ext{AE}\downarrow$	$intra(\mathcal{A}^{ eg F}) \uparrow$	$igg intra(\mathcal{A}^F)\downarrow igg $	$inter(\mathcal{A}^{ eg F})\downarrow$	$inter(\mathcal{A}^F)\uparrow$	time (s) $\downarrow$
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	CCBounds	2.96	0.52	0.03	0.65	0.43	0.43	0.33	3.86
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	SIGNED	NA	NA	NA	NA	NA	NA	NA	$>48\mathrm{h}$
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	SIGNED	NA	NA	NA	NA	NA	NA NA	>48h	
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	SIGNED	41	0.7	0.03	0.61	0.35	0.63		224
	CCBounds	3.28	0.52	0.0007	0.78	0.63	0.45	0.36	4.74
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	SIGNED	NA	NA	NA	NA	NA	NA	NA	>48h
	CCBounds	3.64	0.55	0.0004	0.72	0.55	0.45	0.37	51.1
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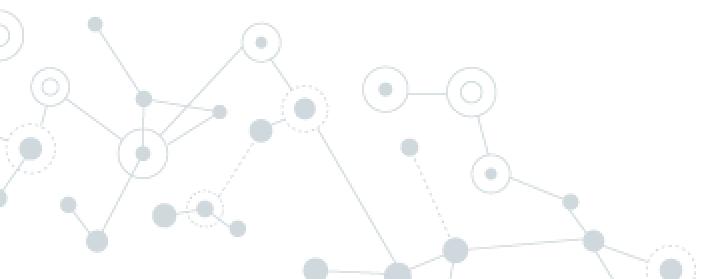
- FAIRLETS, HST-FC and CCBounds guarantee reasonable running times
- CCBounds overcomes its direct competing method SIGNED
- Parallelized pairwise similarity computation
- Abnormal number of clusters for SIGNED



# Results - Running Times

		#clust.	balance ↑	AE↓	$intra(\mathcal{A}^{ eg F})\uparrow$	$intra(\mathcal{A}^F)\downarrow$	$inter(\mathcal{A}^{ eg F})\downarrow$	$inter(\mathcal{A}^F)\uparrow$	time (s) ↓
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	CCBounds	6.44	0.48	0.22	0.65	0.54	0.5	0.38 0.36	4.72
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Diabetes-10k	HST-FC	6	0.799	0.065	0.59	0.388	0.53	0.386	2.84
	SIGNED	NA	NA	NA	NA	NA	NA	0.32 0.337 0.337 NA 0.352 0.385 0.386 0.38 0.36 0.39 0.386 NA OOM OOM OOM OOM OOM	$>48\mathrm{h}$
	CCBounds	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
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#### Conclusions

- We assessed how correlation clustering can handle fair clustering
- Experimental evidence that CCBounds may serve as a good tradeoff between the traditional and fairness-aware clustering conditions

#### **Future Work**

- Alternative definitions of the similarity functions
- Generalization of CCBounds to
  - Multiple protected values
  - Multiple sensitive attributes with many values

# Thanks! Any questions?

You can find me at:



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